

Math 3280 Assignment 12.

- (1) Compute the equilibria of the following nonlinear differential equations, and use that information to match each equation with a trajectory plot from the following page. It may be helpful to compute the eigenvalues at an equilibrium.
- (a) $x' = x - y, y' = x + 3y - 4.$
 - (b) $x' = 2x - y, y' = x - 3y.$
 - (c) $x' = 2 \sin(x) + \sin(y), y' = \sin(x) + 2 \sin(y).$
 - (d) $x' = x - 2y, y' = -x^3 + 4x.$
 - (e) $x' = 1 - y^2, y' = x + 2y.$
 - (f) $x' = x - 2y + 3, y' = x - y + 2.$
- (2) Find the unique equilibrium of the system $x' = x - y, y' = 5x - 3y - 2.$ Compute the eigenvalues of its linearization to determine the stability of the equilibrium (see Theorem 2 in section 9.2).

