Math 3280 Assignment 11, due Thursday, April 13th. This assignment covers material from chapter 10.

(1) Compute the Laplace transform of the function

$$v(t) = \begin{cases} 1 \text{ for } t \in [0, 1] \\ 0 \text{ for } t \in [-\infty, 0) \text{ and } t \in (1, \infty] \end{cases}$$

directly from the definition  $\mathcal{L}(v) = \int_0^\infty e^{-st} v(t) dt$ .

- (2) Use the Laplace transform method to solve the initial value problem x'' x' 2x = 0, x(0) = 0, x'(0) = 1.
- (3) Use the Laplace transform method to solve the initial value problem x' = 2x y, y' = 3x + 4, x(0) = 0, y(0) = 1.
- (4) Use the convolution property of the Laplace transform  $(\mathcal{L}(f*g) = F(s)G(s))$  to compute the inverse transform of  $H = \frac{1}{(s^2+4)^2}$ .
- (5) Compute the Laplace transform of the sawtooth function  $f(t) = t \lfloor t \rfloor$  where  $\lfloor t \rfloor$  is the floor function. The floor of t is the largest integer less than or equal to t. For example,  $\lfloor 2.6 \rfloor = 2$ .