Math 3280 Assignment 7, due Monday February 27th.

For this assignment you should read sections 5.1, 5.2, and 5.3 in the text.

- (1) Compute the Wronskian of $f_1 = e^{-x}$, $f_2 = \cos(x)$ and $f_3 = \sin(x)$ to determine whether these three functions are linearly independent on the real line.
- (2) Solve the initial value problem y'' 4y = 0, y(0) = 4, y'(0) = 2 given that $y_1 = e^{2x}$ and $y_2 = e^{-2x}$ are both solutions to the ODE.
- (3) Find the general solution to y'' + 6y' = 0.
- (4) Find the general solution to 4y'' + 4y' + y = 0.
- (5) For what second-order constant coefficient linear homogeneous ODE would $y = C_1 + C_2 x$ be the general solution?
- (6) Show that the functions 3x, $2x^2$, and $5x 8x^2$ are linearly dependent by finding a linear combination of them that equals zero.
- (7) Find the general solution to y'' + 10y' + 25y = 0.
- (8) Solve the initial value problem y'' 6y' + 25y = 0, y(0) = 6, y'(0) = 2.
- (9) Consider the differential equation y'' + sgn(x)y = 0, where sgn(x) is the sign function:

$$sgn(x) = \begin{cases} 1 & \text{if } x > 0 \\ -1 & \text{if } x < 0 \\ 0 & \text{if } x = 0 \end{cases}$$

Compute the two linearly independent solutions y_1 and y_2 of this differential equation which satisfy the initial conditions $y_1(0) = 1$, $y'_1(0) = 0$ and $y_2(0) = 0$, $y'_2(0) = 1$. (First solve the differential equation for x < 0 and x > 0, and then use the initial conditions to glue them together.)