

Math 3280 Assignment 9, due Thursday, March 23rd.

Find the eigenvalues and eigenvectors of the following matrices:

(1) $\begin{pmatrix} 4 & -2 \\ 1 & 1 \end{pmatrix}$

(2) $\begin{pmatrix} 5 & -6 \\ 3 & -4 \end{pmatrix}$

(3) $\begin{pmatrix} 2 & 0 & 0 \\ 5 & 3 & -2 \\ 2 & 0 & 1 \end{pmatrix}$

(4) $\begin{pmatrix} 3 & 1 & 1 \\ 0 & 1 & 0 \\ 0 & 0 & 1 \end{pmatrix}$

(5) $\begin{pmatrix} 0 & -2 \\ 1 & 0 \end{pmatrix}$

(6) $\begin{pmatrix} 0 & 1 \\ -1 & 0 \end{pmatrix}$

Find a matrix P such that $P^{-1}AP = D$, where D is a diagonal matrix, for the following matrices if such a P exists.

(7) $\begin{pmatrix} 0 & 1 & 0 \\ -1 & 2 & 0 \\ -1 & 1 & 1 \end{pmatrix}$

(8) $\begin{pmatrix} 1 & 0 & 0 & 1 \\ 0 & 1 & 0 & 1 \\ 0 & 0 & 1 & 1 \\ 0 & 0 & 0 & 2 \end{pmatrix}$

(9) Show that if A is invertible and λ is an eigenvalue of A , then $1/\lambda$ is an eigenvalue of A^{-1} . Are the eigenvectors the same?

(10) By computing the eigenvalues and eigenvectors of $A = \begin{pmatrix} 3 & -2 \\ 1 & 0 \end{pmatrix}$ find a matrix P such that $P^{-1}AP = D$ where D is a diagonal matrix. Use this diagonalization to compute A^6 .