Group members (2 to 4):

(1) Using the equation

$$Ax + By + C = x^2 + y^2,$$

find a circle passing through the points (1,7), (-1,3), and (0,0). After finding  $A,\,B,$  and C, put the circle's equation in the standard form

$$(x - c_x)^2 + (y - c_y)^2 = r^2.$$

(by completing the squares).

(2) Find the ellipse of minimal area which is of the form

$$Ax^{2} + 2Bxy + Cy^{2} = (x, y)M\begin{pmatrix} x \\ y \end{pmatrix} = 1$$

where  $M = \begin{pmatrix} A & B \\ B & C \end{pmatrix}$ , and which passes through the points (x,y) = (1,1) and (x,y) = (-1,2).

The area of such an ellipse is  $\frac{\pi}{\sqrt{\det(M)}}$  (note that the minimal area will occur when det(M) is maximized).