Math 3280 Worksheet 14: the Wronskian and review questions

Group members (2 to 4): _____

(1) Compute the Wronskian of the quadratic Bernstein polynomials $f_1 = x^2$, $f_2 = 2x(1-x)$, $f_3 = (1-x)^2$. What can you conclude about their linear independence?

(2) Compute the value of y(1) if $\frac{dy}{dx} = 2xy^2$ and y(0) = 2.

(3) Approximate y(1) from the initial value problem in question (2) by using:

- (a) 1 step of Euler's method
- (b) 1 step of the Improved Euler Method
- (c) 2 steps of the Improved Euler Method

Do these seem to be converging to the correct answer?