

Math 3280 Worksheet 5

Group members (2 to 4): _____

(1) Use Euler's method to estimate $y(1)$ if $y(0) = 1$ and $\frac{dy}{dx} = \frac{y}{2-x} + x^2$, using 1 step.

(2) Again, use Euler's method to estimate $y(1)$ if $y(0) = 1$ and $\frac{dy}{dx} = \frac{y}{2-x} + x^2$, but using 2 steps.

(3) Now use 4 steps for the same problem as before.

- (4) Find the exact value of $y(1)$ by solving the initial value problem (note that the ODE is linear).
- (5) Use two steps of the improved Euler method to approximate the same problem as before. Is this more accurate than using 4 steps of Euler's method?