(1) Compute the divergence of the curl of $\vec{F} = (xy^2, xyz, x)$.

(2) Construct a vector field \vec{G} such that $\operatorname{curl}(\vec{G}) = (1,0,0)$ and each component of \vec{G} is non-constant.

(3) Can you find a function f(x, y, z) for which the $\operatorname{curl}(\nabla f) \neq 0$?