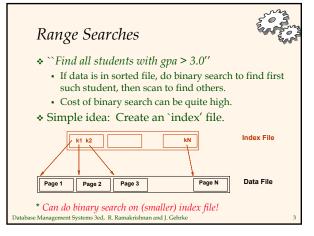
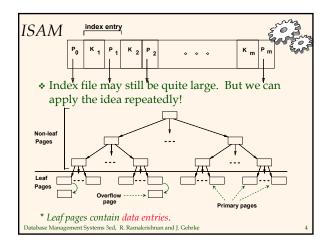


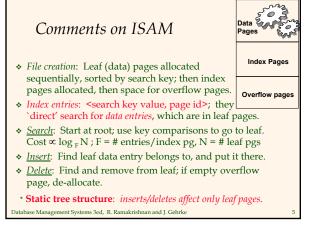
## Introduction

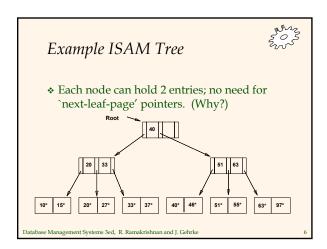
- ❖ As for any index, 3 alternatives for data entries k\*:
  - Data record with key value k
  - <k, rid of data record with search key value k>
  - <k, list of rids of data records with search key k>
- Choice is orthogonal to the *indexing technique* used to locate data entries k\*.
- \* Tree-structured indexing techniques support both *range searches* and *equality searches*.
- \* <u>ISAM</u>: static structure; <u>B+ tree</u>: dynamic, adjusts gracefully under inserts and deletes.

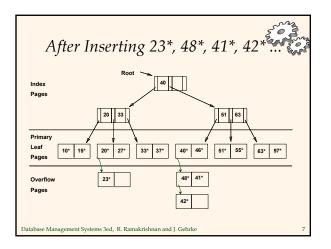
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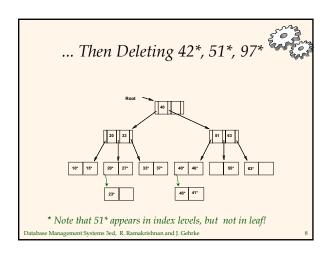






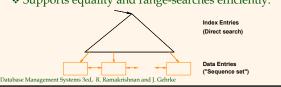






## B+ Tree: Most Widely Used Index

- Insert/delete at log F N cost; keep tree heightbalanced. (F = fanout, N = # leaf pages)
- ❖ Minimum 50% occupancy (except for root). Each node contains d <= m <= 2d entries. The parameter d is called the *order* of the tree.
- \* Supports equality and range-searches efficiently.



## Example B+ Tree

- Search begins at root, and key comparisons direct it to a leaf (as in ISAM).
- ❖ Search for 5\*, 15\*, all data entries >= 24\* ...



## B+ Trees in Practice

- \* Typical order: 100. Typical fill-factor: 67%.
  - average fanout = 133
- Typical capacities:
  - Height 4: 133<sup>4</sup> = 312,900,700 records
  - Height 3: 133<sup>3</sup> = 2,352,637 records
- \* Can often hold top levels in buffer pool:
  - Level 1 = 1 page = 8 Kbytes
  - Level 2 = 133 pages = 1 Mbyte
  - Level 3 = 17,689 pages = 133 MBytes

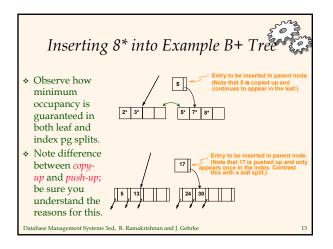
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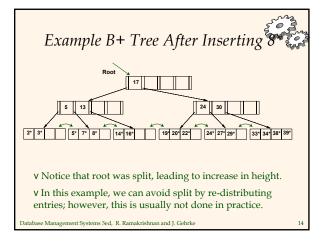
## Inserting a Data Entry into a B+ Tre



- ❖ Find correct leaf L.
- ❖ Put data entry onto *L*.
  - If *L* has enough space, *done*!
  - Else, must <u>split</u> L (into L and a new node L2)
    - Redistribute entries evenly, copy up middle key.
    - Insert index entry pointing to L2 into parent of L.
- This can happen recursively
  - To split index node, redistribute entries evenly, but push up middle key. (Contrast with leaf splits.)
- Splits "grow" tree; root split increases height.
  - Tree growth: gets wider or one level taller at top.

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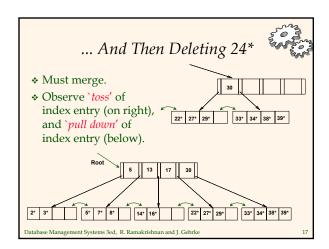


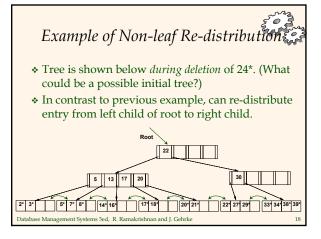
## Deleting a Data Entry from a B+ T

- ❖ Start at root, find leaf *L* where entry belongs.
- \* Remove the entry.
  - If L is at least half-full, done!
  - If L has only **d-1** entries,
    - Try to re-distribute, borrowing from <u>sibling</u> (adjacent node with same parent as L).
    - If re-distribution fails, <u>merge</u> L and sibling.
- ❖ If merge occurred, must delete entry (pointing to L or sibling) from parent of L.
- Merge could propagate to root, decreasing height.

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# Example Tree After (Inserting 8\*5 Then) Deleting 19\* and 20\* ... Root 17 27 30 27 30 30 32 33 34 38 39 Deleting 19\* is easy. Deleting 20\* is done with re-distribution. Notice how middle key is copied up. Database Management Systems 3ed, R. Ramakrishnan and J. Gebrke Database Management Systems 3ed, R. Ramakrishnan and J. Gebrke





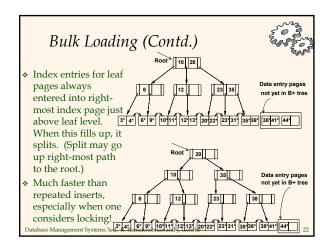
## \* Intuitively, entries are re-distributed by `pushing through' the splitting entry in the parent node. \* It suffices to re-distribute index entry with key 20; we've re-distributed 17 as well for illustration.

## Prefix Key Compression

- Important to increase fan-out. (Why?)
- Key values in index entries only `direct traffic'; can often compress them.
  - E.g., If we have adjacent index entries with search key values *Dannon Yogurt*, *David Smith* and *Devarakonda Murthy*, we can abbreviate *David Smith* to *Dav*. (The other keys can be compressed too ...)
    - Is this correct? Not quite! What if there is a data entry Davey Jones? (Can only compress David Smith to Davi)
    - In general, while compressing, must leave each index entry greater than every key value (in any subtree) to its left.
- Insert/delete must be suitably modified.

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## \* If we have a large collection of records, and we want to create a B+ tree on some field, doing so by repeatedly inserting records is very slow. \* \* \* \* Bulk Loading\*\* can be done much more efficiently. \* \* Initialization: Sort all data entries, insert pointer to first (leaf) page in a new (root) page. \*\* \*\*Sorted pages of data entries; not yet in B+ tree\* \*\*Sorted pages of data entries; not yet in B+ tree\* \*\* \*\*Sorted pages of data entries; not yet in B+ tree\* \*\*Sorted pages of data entries; not yet in B+ tree\*



## Summary of Bulk Loading



Option 1: multiple inserts.

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- Slow
- Does not give sequential storage of leaves.
- Option 2: Bulk Loading
  - Has advantages for concurrency control.
  - Fewer I/Os during build.
  - Leaves will be stored sequentially (and linked, of course).
  - · Can control "fill factor" on pages.

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## A Note on `Order'



- \* Order (d) concept replaced by physical space criterion in practice (`at least half-full').
  - Index pages can typically hold many more entries than leaf pages.
  - Variable sized records and search keys mean differnt nodes will contain different numbers of entries.
  - Even with fixed length fields, multiple records with the same search key value (duplicates) can lead to variable-sized data entries (if we use Alternative (3)).

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## Summary

- Tree-structured indexes are ideal for rangesearches, also good for equality searches.
- \* ISAM is a static structure.
  - Only leaf pages modified; overflow pages needed.
  - Overflow chains can degrade performance unless size of data set and data distribution stay constant.
- \* B+ tree is a dynamic structure.
  - Inserts/deletes leave tree height-balanced; log F N cost.
  - High fanout (F) means depth rarely more than 3 or 4.
  - Almost always better than maintaining a sorted file.

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## Summary (Contd.)

- Typically, 67% occupancy on average.
- Usually preferable to ISAM, modulo *locking* considerations; adjusts to growth gracefully.
- If data entries are data records, splits can change rids!
- \* Key compression increases fanout, reduces height.
- Bulk loading can be much faster than repeated inserts for creating a B+ tree on a large data set.
- Most widely used index in database management systems because of its versatility. One of the most optimized components of a DBMS.

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