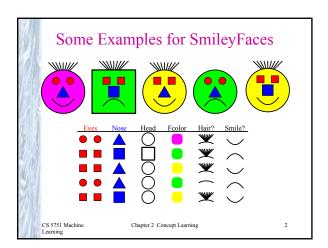
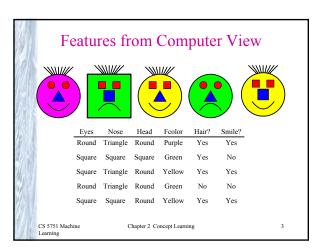
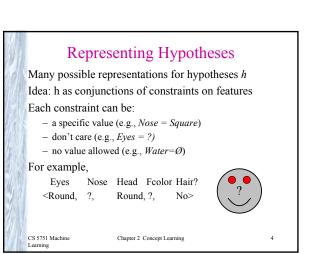
# **Concept Learning**

- · Learning from examples
- General-to-specific ordering over hypotheses
- Version Spaces and candidate elimination algorithm
- · Picking new examples
- · The need for inductive bias

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# Prototypical Concept Learning Task

## Given:

- Instances *X*: Faces, each described by the attributes *Eyes*, *Nose*, *Head*, *Fcolor*, and *Hair*?
- Target function c: Smile? :  $X \rightarrow \{ \text{ no, yes } \}$
- Hypotheses H: Conjunctions of literals such as <?,Square,Square,Yellow,?>
- Training examples *D*: Positive and negative examples of the target function

$$< x_1, c(x_1) >, < x_2, c(x_2) >, ..., < x_m, c(x_m) >$$

**Determine:** a hypothesis h in H such that h(x)=c(x) for all x in D.

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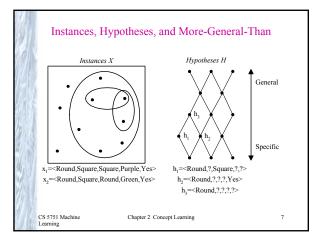
# **Inductive Learning Hypothesis**

Any hypothesis found to approximate the target function well over a sufficiently large set of training examples will also approximate the target function well over other unobserved examples.

- What are the implications?
- Is this reasonable?
- What (if any) are our alternatives?
- What about concept drift (what if our views/tastes change over time)?

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# ${\tt Find-S} \ Algorithm$

- 1. Initialize h to the most specific hypothesis in H
- 2. For each positive training instance x

For each attribute constraint  $a_i$  in hIF the constraint  $a_i$  in h is satisfied by x THEN do nothing

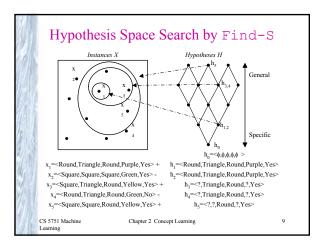
ELSE

replace  $a_i$  in h by next more general constraint satisfied by x

3. Output hypothesis h

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# Complaints about Find-S

- · Cannot tell whether it has learned concept
- · Cannot tell when training data inconsistent
- Picks a maximally specific h (why?)
- Depending on *H*, there might be several!
- How do we fix this?

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## The List-Then-Eliminate Algorithm

- 1. Set *VersionSpace* equal to a list containing every hypothesis in *H*
- 2. For each training example,  $\langle x, c(x) \rangle$  remove from *VersionSpace* any hypothesis *h* for which h(x) != c(x)
- 3. Output the list of hypotheses in VersionSpace
- But is listing all hypotheses reasonable?
- How many different hypotheses in our simple problem?
  - How many not involving "?" terms?

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# **Version Spaces**

A hypothesis h is **consistent** with a set of training examples D of target concept c if and only if h(x)=c(x) for each training example in D.

Consistent 
$$(h, D) \equiv (\forall \langle x, c(x) \rangle \in D) h(x) = c(x)$$

The **version space**,  $VS_{H,D}$ , with respect to hypothesis space H and training examples D, is the subset of hypotheses from H consistent with all training examples in D.

$$VS_{H,D} \equiv \{h \in H \mid Consistent(h, D)\}$$

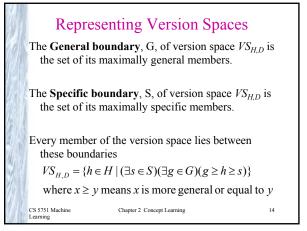
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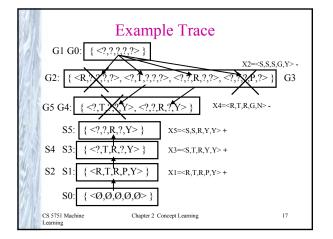
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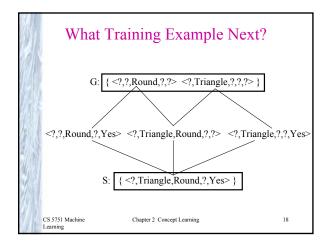
# Example Version Space G: {<?,?,Round,?,?> <?,Triangle,?,?,?>} <?,?,Round,?,Yes> <?,Triangle,Round,?,?> <?,Triangle,?,?,Yes> S: {<?,Triangle,Round,?,Yes>}

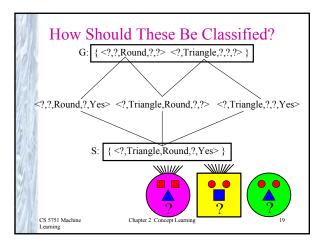


# Candidate Elimination Algorithm G = maximally general hypotheses in H S = maximally specific hypotheses in H For each training example d, do If d is a positive example Remove from G any hypothesis that does not include d For each hypothesis s in S that does not include d Remove s from S Add to S all minimal generalizations h of s such that 1. h includes d, and 2. Some member of G is more general than h Remove from S any hypothesis that is more general than another hypothesis in S

# Candidate Elimination Algorithm (cont) For each training example d, do (cont) If d is a negative example Remove from S any hypothesis that does include d For each hypothesis g in G that does include d Remove g from G Add to G all minimal generalizations h of g such that 1. h does not include d, and 2. Some member of S is more specific than h Remove from G any hypothesis that is less general than another hypothesis in G If G or S ever becomes empty, data not consistent (with H)







# What Justifies this Inductive Leap?

- + < Round, Triangle, Round, Purple, Yes >
- + < Square, Triangle, Round, Yellow, Yes >

S: <?, Triangle, Round,?, Yes>

Why believe we can classify the unseen?

< Square, Triangle, Round, Purple, Yes >?

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## An UN-Biased Learner

Idea: Choose *H* that expresses every teachable concept (i.e., *H* is the power set of *X*)

Consider *H'* = disjunctions, conjunctions, negations over previous *H*.

For example:

<?, Triangle, Round, ?,  $Yes > \lor < Square$ , Square, ?, Purple,  $? > \lor$ 

What are S, G, in this case?

Learning

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## **Inductive Bias**

## Consider

- concept learning algorithm L
- instances X, target concept c
- training examples  $D_c = \{ \langle x, c(x) \rangle \}$
- let  $L(x_p D_o)$  denote the classification assigned to the instance  $x_i$  by L after training on data  $D_o$ .

### Definition:

The **inductive bias** of L is any minimal set of assertions B such that for any target concept c and corresponding training examples  $D_c$ 

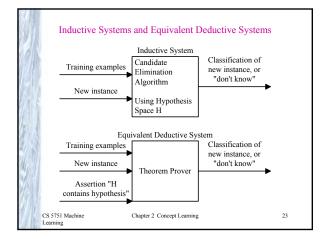
$$(\forall x_i \in X)[(B \land D_c \land x_i) \vdash L(x_i, D_c)]$$

where  $A \vdash B$  means A logically entails B

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## Three Learners with Different Biases

- Rote learner: store examples, classify new instance iff it matches previously observed example (don't know otherwise).
- 2. Version space candidate elimination algorithm.
- 3. Find-S

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# **Summary Points**

- 1. Concept learning as search through H
- 2. General-to-specific ordering over H
- 3. Version space candidate elimination algorithm
- 4. *S* and *G* boundaries characterize learner's uncertainty
- 5. Learner can generate useful queries
- 6. Inductive leaps possible only if learner is biased
- 7. Inductive learners can be modeled by equivalent deductive systems

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