## Clustering

- · Unsupervised learning
- · Generating "classes"
- · Distance/similarity measures
- · Agglomerative methods
- · Divisive methods

CS 5751 Machine Learning Data Clustering

## What is Clustering?

- Form of *unsupervised* learning no information from teacher
- The process of partitioning a set of data into a set of meaningful (hopefully) sub-classes, called clusters
- Cluster:
  - collection of data points that are "similar" to one another and collectively should be treated as group
  - as a collection, are sufficiently different from other groups

CS 5751 Machine Learning Data Clustering

Clusters

CS 5751 Machine
Learning

Data Clustering

3

## **Characterizing Cluster Methods**

- · Class label applied by clustering algorithm
  - hard versus fuzzy:
    - hard either is or is not a member of cluster
    - · fuzzy member of cluster with probability
- Distance (similarity) measure value indicating how similar data points are
- · Deterministic versus stochastic
  - deterministic same clusters produced every time
  - stochastic different clusters may result
- Hierarchical points connected into clusters using a hierarchical structure

CS 5751 Machine

Data Clustering

# Basic Clustering Methodology

## Two approaches:

Agglomerative: pairs of items/clusters are successively linked to produce larger clusters

Divisive (partitioning): items are initially placed in one cluster and successively divided into separate groups

CS 5751 Machine Learning Data Clustering

## **Cluster Validity**

- One difficult question: how *good* are the clusters produced by a particular algorithm?
- Difficult to develop an objective measure
- Some approaches:
  - external assessment: compare clustering to a priori clustering
  - internal assessment: determine if clustering intrinsically appropriate for data
  - relative assessment: compare one clustering methods results to another methods

CS 5751 Machine

Data Clustering

## **Basic Ouestions**

- Data preparation getting/setting up data for clustering
  - extraction
  - normalization
- Similarity/Distance measure how is the distance between points defined
- Use of domain knowledge (prior knowledge)
  - can influence preparation, Similarity/Distance measure
- Efficiency how to construct clusters in a reasonable amount of time

CS 5751 Machine Learning Data Clustering

7

### Distance/Similarity Measures · Key to grouping points distance = inverse of similarity · Often based on representation of objects as feature vectors Term Frequencies for Documents An Employee DB T5 T6 ID Gender Age Salary 19.000 Doc2 3 2 2 M 51 64.000 0 0 0 3 0 Doc3 3 M 52 100.000 0 3 Doc4 4 F 33 55.000 Doc5 M 45 45,000 Which objects are more similar? CS 5751 Machine Data Clustering

## Distance/Similarity Measures

### Properties of measures:

based on feature values  $x_{instance\#,feature\#}$  for all objects  $x_i$ ,B,  $\operatorname{dist}(x_i, x_j) \ge 0$ ,  $\operatorname{dist}(x_i, x_j) = \operatorname{dist}(x_j, x_i)$  for any object  $x_i$ ,  $\operatorname{dist}(x_i, x_i) = 0$   $\operatorname{dist}(x_i, x_i) \le \operatorname{dist}(x_i, x_k) + \operatorname{dist}(x_k, x_i)$ 

Manhattan distance: |feat

 $\sum_{f=1}^{atures|} |x_{i,f} - x_{j,f}|$ 

Euclidean distance:

 $\sqrt{\sum_{f=1}^{|features|} (x_{i,f} - x_{j,f})^2}$ 

CS 5751 Machine

ering

## Distance/Similarity Measures

Minkowski distance (p):

$$\sqrt[p]{\sum_{f=1}^{|features|}(x_{i,f}-x_{j,f})^p}$$

Mahalanobis distance:  $(x_i - x_j)\nabla^{-1}(x_i - x_j)^T$ where  $\nabla^{-1}$  is covariance matrix of the patterns

More complex measures:

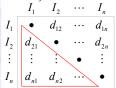
Mutual Neighbor Distance (MND) - based on a count of number of neighbors

CS 5751 Machine Learning

a Clustering

# Distance (Similarity) Matrix

- Similarity (Distance) Matrix
  - based on the distance or similarity measure we can construct a symmetric matrix of distance (or similarity values)
  - (i, j) entry in the matrix is the distance (similarity) between items i
    and j



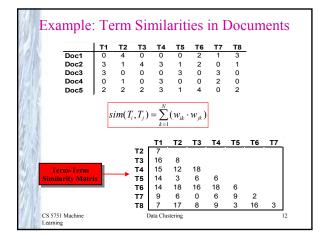
Note that  $d_{ij} = d_{ji}$  (i.e., the matrix is symmetric). So, we only need the lower triangle part of the matrix.

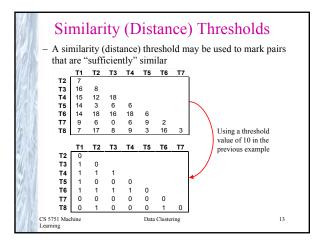
The diagonal is all 1's (similarity) or all 0's (distance)

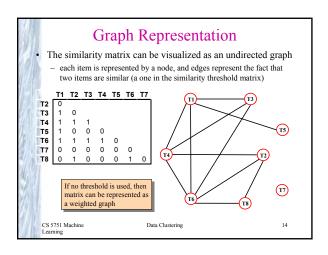
11

 $d_{ij} = \text{similarity (or distance) of } D_i \text{ to } D_j$ 

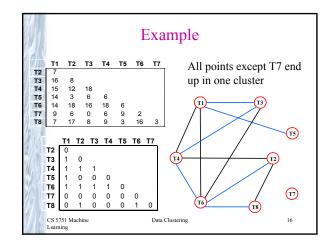
CS 5751 Machine Learning Data Clustering



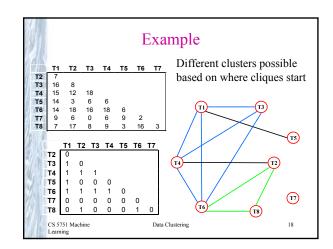




# Agglomerative Single-Link • Single-link: connect all points together that are within a threshold distance • Algorithm: 1. place all points in a cluster 2. pick a point to start a cluster 3. for each point in current cluster add all points within threshold not already in cluster repeat until no more items added to cluster 4. remove points in current cluster from graph 5. Repeat step 2 until no more points in graph



# Agglomerative Complete-Link (Clique) Complete-link (clique): all of the points in a cluster must be within the threshold distance In the threshold distance matrix, a clique is a complete graph Algorithms based on finding maximal cliques (once a point is chosen, pick the largest clique it is part of) not an easy problem



# Hierarchical Methods • Based on some method of representing hierarchy of data points • One idea: hierarchical dendogram (connects points based on similarity) T1 T2 T3 T4 T5 T6 T7 T3 16 8 T4 15 12 18 T5 14 3 6 6 T6 14 18 16 18 6 T7 9 6 0 0 6 9 9 2 T8 7 17 8 9 3 16 3 CS 5751 Machine Learning Data Clustering

## Hierarchical Agglomerative

- Compute distance matrix
- · Put each data point in its own cluster
- Find most similar pair of clusters
  - merge pairs of clusters (show merger in dendogram)
  - update proximity matrix
  - repeat until all patterns in one cluster

CS 5751 Machine Learning Data Clustering

Data Crastering 20

## Partitional Methods

- Divide data points into a number of clusters
- · Difficult questions
  - how many clusters?
  - how to divide the points?
  - how to represent cluster?
- Representing cluster: often done in terms of centroid for cluster
  - centroid of cluster minimizes squared distance between the centroid and all points in cluster

CS 5751 Machine Learning Data Clustering

## k-Means Clustering

- 1. Choose *k* cluster centers (randomly pick k data points as center, or randomly distribute in space)
- 2. Assign each pattern to the closest cluster center
- Recompute the cluster centers using the current cluster memberships (moving centers may change memberships)
- 4. If a convergence criterion is not met, goto step 2

## Convergence criterion:

- no reassignment of patterns
- minimal change in cluster center

CS 5751 Machine

Data Clustering

22

20

# 

## k-Means Variations

- What if too many/not enough clusters?
- · After some convergence:
  - any cluster with too large a distance between members is split
  - any clusters too close together are combined
  - any cluster not corresponding to any points is moved
  - thresholds decided empirically

CS 5751 Machine

Data Clustering

24

## An Incremental Clustering Algorithm

- 1. Assign first data point to a cluster
- Consider next data point. Either assign data point to an existing cluster or create a new cluster.
   Assignment to cluster based on threshold
- 3. Repeat step 2 until all points are clustered

Useful for efficient clustering

CS 5751 Machine Learning Data Clustering

25

## **Clustering Summary**

- · Unsupervised learning method
  - generation of "classes"
- · Based on similarity/distance measure
  - Manhattan, Euclidean, Minkowski, Mahalanobis, etc.
  - distance matrix
  - threshold distance matrix
- Hierarchical representation
  - hierarchical dendogram
- Agglomerative methods
  - single link
  - complete link (clique)

CS 5751 Machine Data Clustering Learning

26

# **Clustering Summary**

- · Partitional method
  - representing clusters
    - · centroids and "error"
  - k-Means clustering
    - · combining/splitting k-Means
- · Incremental clustering
  - one pass clustering

CS 5751 Machine Learning Data Clustering

27