

Phys2021

#6. Derive the average energy  $E_{avg}=kT$  for a classical oscillator from their classical energy distribution: According to the Boltzmann distribution, the probability for an oscillator to have energy  $E$  is  $P(E) = A_0 \exp(-E/kT)$ , where  $k$  is the Boltzmann constant and  $A_0$  is some number (the normalization constant). That is, if you have a very large number of oscillators and want to know how many of them have energies in some small interval between  $E$  and  $E+dE$ , that number is  $N(E) = P(E)dE = A_0 \exp(-E/kT)dE$ . Your task is to calculate the average energy per oscillator.

*Hint:* The average energy is the total energy of the system divided by the number of oscillators.