Math 3280: DE+LA. Test 2 partial answers. Prof. Bruce Peckham

- 1. (a) $y(x) = c_1 e^x + c_2 e^{-4x}$ (b) $y(x) = c_1 e^{2x} + c_2 x e^{2x}$ 2. $y(x) = \frac{7}{4} e^{2x} + \frac{5}{4} e^{-2x} - 2$ 3. (a) 63 (b) 79 4. 32 5. $(x_1, x_2, x_3) = (\frac{1}{3}, 1, -\frac{1}{3})$ $\left(\begin{pmatrix} 5\\ 2 \end{pmatrix}\right)$
- 6. $\left\{ \begin{pmatrix} 5\\ -2\\ 1\\ 1 \end{pmatrix} \right\}$ (or any multiple of this vector)
- 7. Basis: $\left\{ \begin{pmatrix} 1\\2 \end{pmatrix}, \begin{pmatrix} 2\\5 \end{pmatrix} \right\}$ (or any two of the three given vectors, or any two independent vectors in \Re^2 , since the span of the three given vectors is all of \Re^2 .

8. (a)
$$A^{-1} = \begin{pmatrix} 1 & 0 & 0 \\ 2 & 1 & 0 \\ 0 & 0 & \frac{1}{3} \end{pmatrix}$$

(b) Multiply row three by 3; replace row 2 with itself - 2 times row 1.

- 9. (a) True (b) False (c) False
- 10. Yes. Closed under both multiplication by scalars and addition of vectors.
- 11. On previous class handout
- 12. On previous class handout