Math 3280 Worksheet 33: first-order systems
Group members (1 to 4): $\qquad$
(1) Solve the initial value problem

$$
\begin{gathered}
x_{1}^{\prime}=x_{1}+2 x_{2} \\
x_{2}^{\prime}=-2 x_{1}+x_{2} \\
x_{1}(0)=1 \\
x_{2}(0)=2 .
\end{gathered}
$$

(2) Approximate the value of $x_{1}(0.5)$ and $x_{2}(0.5)$ for the system $x_{1}^{\prime}=x_{1}+2 x_{2}$, $x_{2}^{\prime}=-2 x_{1}+x_{2}$ if $x_{1}(0)=1$ and $x_{2}(0)=2$ using Euler's method with 2 steps.
(3) Compare your answer above to the exact solution from (1), and indicate on the vector field plot both the approximate and exact points.


