(1) Find the area of the region bounded by the curves $y = x$, $y = 2x$, $xy = 1$, and $xy = 2$ by changing coordinates to $u = xy$, $v = y/x$. 