



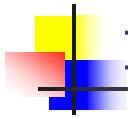
Intermediate Code and Optimizations

- We have discussed
 - Runtime organization
 - Simple stack machine code generation
 - Improvements to stack machine code generation
- Our compiler goes directly from AST to assembly language
 - And does not perform optimizations
- Most real compilers use intermediate languages



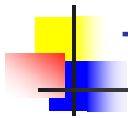
Why Intermediate Languages ?

- When to perform optimizations
 - On AST
 - **Pro:** Machine independent
 - **Con:** Too high level
 - On assembly language
 - **Pro:** Exposes optimization opportunities
 - **Con:** Machine dependent
 - **Con:** Must re-implement optimizations when re-targetting
 - On an intermediate language
 - **Pro:** Machine independent
 - **Pro:** Exposes optimization opportunities



Intermediate Languages

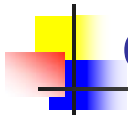
- Each compiler uses its own intermediate language
 - IL design is still an active area of research
- Intermediate language = high-level assembly language
 - Uses register names, but has an unlimited number
 - Uses control structures like assembly language
 - Uses op-codes but some are higher level
 - E.g., `push` translates to several assembly instructions
 - Most op-codes correspond directly to assembly op-codes



Three-Address Intermediate Code

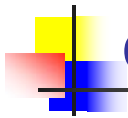
- Each instruction is of the form
$$x := y \text{ op } z$$
 - `y` and `z` can be only registers or constants
 - Just like assembly
- Common form of intermediate code
- The AST expression `x + y * z` is translated as

$$t_1 := y * z$$



Generating Intermediate Code

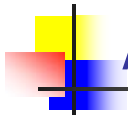
- Similar to assembly code generation
- Major difference
 - Use any number of IL registers to hold intermediate results



Generating Int. Code (Cont.)

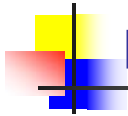
- **Igen(e, t)** function generates code to compute the value of **e** in register **t**
- Example:
$$\text{igen}(e_1 + e_2, t) =$$

$\text{igen}(e_1, t_1)$	(t_1 is a fresh register)
$\text{igen}(e_2, t_2)$	(t_2 is a fresh register)
$t := t_1 + t_2$	
- Unlimited number of registers
⇒ simple code generation



An Intermediate Language

- $P \rightarrow S P \mid \varepsilon$ • id's are register names
- $S \rightarrow id := id \text{ op } id$ • Constants can replace id's
- | $id := op \ id$ • Typical operators: +, -, *
- | $id := id$
- | push id
- | $id := pop$
- | if id relop id goto L
- | L:
- | jump L



Definition: Basic Blocks

- A basic block is a maximal sequence of instructions with:
 - no labels (except at the first instruction), and
 - no jumps (except in the last instruction)
- Idea:
 - Cannot jump into a basic block (except at beginning)
 - Cannot jump out of a basic block (except at end)
 - Each instruction in a basic block is executed after all the preceding instructions have been executed



Basic Block Example

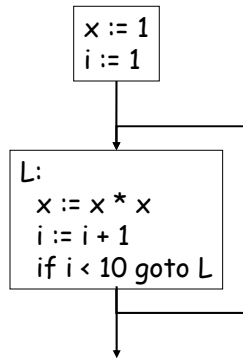
- Consider the basic block
 1. L:
 2. $t := 2 * x$
 3. $w := t + x$
 4. if $w > 0$ goto L
- No way for (3) to be executed without (2) having been executed right before
 - We know we can change (3) to $w := 3 * x$
 - Can we eliminate (2) as well?



Definition. Control-Flow Graphs

- A control-flow graph is a directed graph with
 - Basic blocks as nodes
 - An edge from block A to block B if the execution can flow from the last instruction in A to the first instruction in B
 - E.g., the last instruction in A is jump L_B
 - E.g., the execution can fall-through from block A to block B

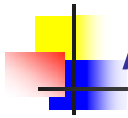
Control-Flow Graphs. Example.



- The body of a method (or procedure) can be represented as a control-flow graph
- There is one initial node
- All "return" nodes are terminal

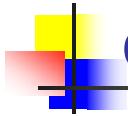
Optimization Overview

- Optimization seeks to improve a program's utilization of some resource
 - Execution time (most often)
 - Code size
 - Network messages sent, etc.
- Optimization should not alter what the program computes
 - The answer must still be the same



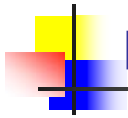
A Classification of Optimizations

- For languages like C and Java there are three granularities of optimizations
 1. Local optimizations
 - Apply to a basic block in isolation
 2. Global optimizations
 - Apply to a control-flow graph (method body) in isolation
 3. Inter-procedural optimizations
 - Apply across method boundaries
- Most compilers do (1), many do (2) and very few do (3)



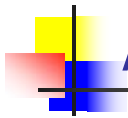
Cost of Optimizations

- In practice, a conscious decision is made not to implement the fanciest optimization known
- Why?
 - Some optimizations are hard to implement
 - Some optimizations are costly in terms of compilation time
 - The fancy optimizations are both hard and costly
- The goal: maximum improvement with minimum of cost



Local Optimizations

- The simplest form of optimizations
- No need to analyze the whole procedure body
 - Just the basic block in question
- Example: algebraic simplification



Algebraic Simplification

- Some statements can be deleted

`x := x + 0`

`x := x * 1`

- Some statements can be simplified

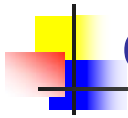
`x := x * 0` \Rightarrow `x := 0`

`y := y ** 2` \Rightarrow `y := y * y`

`x := x * 8` \Rightarrow `x := x << 3`

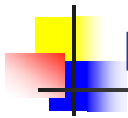
`x := x * 15` \Rightarrow `t := x << 4; x := t - x`

(on some machines << is faster than *; but not on all!)



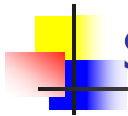
Constant Folding

- Operations on constants can be computed at compile time
- In general, if there is a statement
$$x := y \text{ op } z$$
 - And y and z are constants
 - Then y op z can be computed at compile time
- Example: $x := 2 + 2 \Rightarrow x := 4$
- Example: $\text{if } 2 < 0 \text{ jump } L$ can be deleted
- When might constant folding be dangerous?



Flow of Control Optimizations

- Eliminating unreachable code:
 - Code that is unreachable in the control-flow graph
 - Basic blocks that are not the target of any jump or “fall through” from a conditional
 - Such basic blocks can be eliminated
- Why would such basic blocks occur?
- Removing unreachable code makes the program smaller
 - And sometimes also faster
 - Due to memory cache effects (increased spatial locality)



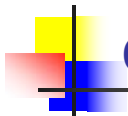
Single Assignment Form

- Some optimizations are simplified if each register occurs only once on the left-hand side of an assignment
- Intermediate code can be rewritten to be in single assignment form

$x := z + y$		$b := z + y$
$a := x$	\Rightarrow	$a := b$
$x := 2 * x$		$x := 2 * b$

(b is a fresh register)

- More complicated in general, due to loops



Common Sub-expression Elimination

- Assume
 - Basic block is in single assignment form
 - A definition $x :=$ is the first use of x in a block
- If any assignment have the same rhs, they compute the same value

- Example:

$x := y + z$		$x := y + z$
...	\Rightarrow	...
$w := y + z$		$w := x$

(the values of x , y , and z do not change in the ... code)



Copy Propagation

- If $w := x$ appears in a block, all subsequent uses of w can be replaced with uses of x
- Example:

$b := z + y$		$b := z + y$
$a := b$	\Rightarrow	$a := b$
$x := 2 * a$		$x := 2 * b$
- This does not make the program smaller or faster but might enable other optimizations
 - Constant folding
 - Dead code elimination



Copy Propagation and Constant Folding

- Example:

$a := 5$		$a := 5$
$x := 2 * a$	\Rightarrow	$x := 10$
$y := x + 6$		$y := 16$
$t := x * y$		$t := x << 4$



Copy Propagation and Dead Code Elimination

If

$w := rhs$ appears in a basic block
 w does not appear anywhere else in the program

Then

the statement $w := rhs$ is dead and can be eliminated

- Dead = does not contribute to the program's result

Example: (a is not used anywhere else)

$x := z + y$		$b := z + y$		$b := x + y$
$a := x$	\Rightarrow	$a := b$	\Rightarrow	$x := 2 * b$
$x := 2 * x$		$x := 2 * b$		



Applying Local Optimizations

- Each local optimization does very little by itself
- Typically optimizations interact
 - Performing one optimization enables other optimizations
- Typical optimizing compilers repeatedly perform optimizations until no improvement is possible
 - The optimizer can also be stopped at any time to limit the compilation time



An Example

- Initial code:

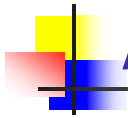
```
a := x ** 2
b := 3
c := x
d := c * c
e := b * 2
f := a + d
g := e * f
```



An Example

- Algebraic optimization:

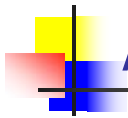
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An Example

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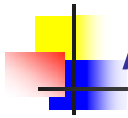
```
a := x * x
b := 3
c := x
d := c * c
e := b << 1
f := a + d
g := e * f
```



An Example

- Copy propagation:

```
a := x * x
b := 3
c := x
d := c * c
e := b << 1
f := a + d
g := e * f
```



An Example

- Copy propagation:

a := x * x

b := 3

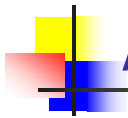
c := x

d := x * x

e := 3 << 1

f := a + d

g := e * f



An Example

- Constant folding:

a := x * x

b := 3

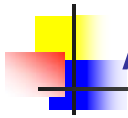
c := x

d := x * x

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An Example

- Constant folding:

a := x * x

b := 3

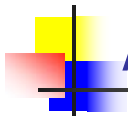
c := x

d := x * x

e := 6

f := a + d

g := e * f



An Example

- Common subexpression elimination:

a := x * x

b := 3

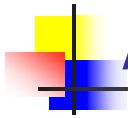
c := x

d := x * x

e := 6

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g := e * f



An Example

- Common subexpression elimination:

a := x * x

b := 3

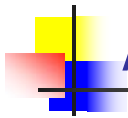
c := x

d := a

e := 6

f := a + d

g := e * f



An Example

- Copy propagation:

a := x * x

b := 3

c := x

d := a

e := 6

f := a + d

g := e * f



An Example

- Copy propagation:

a := x * x

b := 3

c := x

d := a

e := 6

f := a + a

g := 6 * f



An Example

- Dead code elimination:

a := x * x

b := 3

c := x

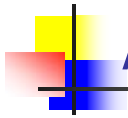
d := a

e := 6

f := a + a

g := 6 * f

Note: assume b, c, d, e are temporaries
(introduced by the compiler) and hence are not
used outside this basic block



An Example

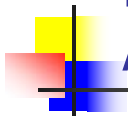
- Dead code elimination:

$a := x * x$

$f := a + a$

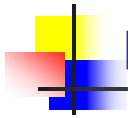
$g := 6 * f$

- This is the final form



Peephole Optimizations on Assembly Code

- The optimizations presented before work on intermediate code
 - They are target independent
 - But they can be applied on assembly language also
- Peephole optimization is an effective technique for improving assembly code
 - The “peephole” is a short sequence of (usually contiguous) instructions
 - The optimizer replaces the sequence with another equivalent one (but faster)



Peephole Optimizations (Cont.)

- Write peephole optimizations as replacement rules

$$i_1, \dots, i_n \rightarrow j_1, \dots, j_m$$

where the rhs is the improved version of the lhs

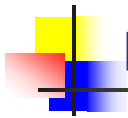
- Example:

move \$a \$b, move \$b \$a → move \$a \$b

- Works if move \$b \$a is not the target of a jump

- Another example

addiu \$a \$a i, addiu \$a \$a j → addiu \$a \$a i+j



Peephole Optimizations (Cont.)

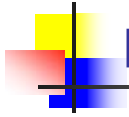
- Many (but not all) of the basic block optimizations can be cast as peephole optimizations

- Example: addiu \$a \$b 0 → move \$a \$b

- Example: move \$a \$a →

- These two together eliminate addiu \$a \$a 0

- Just like for local optimizations, peephole optimizations need to be applied repeatedly to get maximum effect



Local Optimizations. Notes.

- Intermediate code is helpful for many optimizations
- Many simple optimizations can still be applied on assembly language
- “Program optimization” is grossly misnamed
 - Code produced by “optimizers” is not optimal in any reasonable sense
 - “Program improvement” is a more appropriate term