## Math 3280 Assignment 2, due Wednesday, February 5th.

In addition to the problems below, you should read sections 1.3, 1.4, and 1.5 in our text.

Find the general solutions y(x) to the following separable equations:

(1) 
$$y' = 4xy$$
.

$$(2) (2 + 2x)y' = 4y.$$

(3) 
$$y' = y \cos(x)$$
.

(4) 
$$y' = 1 + x + y + xy$$
.

Find the solution y(x) to the following initial value problems:

(5) 
$$y' = 2ye^x$$
,  $y(0) = 2e^2$ .

(6) 
$$y' = x^3(y^2 + 1), y(0) = 1.$$

(7) In carbon-dating organic material it is assumed that the amount of carbon-14 ( $^{14}C$ ) decays exponentially ( $\frac{d^{-14}C}{dt} = -k^{-14}C$ ) with rate constant of  $k \approx 0.0001216$  where t is measured in years. Suppose an archeological bone sample contains 1/7 as much carbon-14 as is in a present-day sample. How old is the bone?

Determine what the existence and uniqueness theorem (Theorem 1 from Chapter 1.3) guarantees about solutions to the following initial value problems (note that you do not have to find the solutions):

(8) 
$$dy/dx = \sqrt{xy}, y(0) = 1.$$

(9) 
$$dy/dx = y^{1/3}, y(0) = 2.$$

(10) 
$$dy/dx = y^{1/3}, y(2) = 0.$$

(11) 
$$dy/dx = x \ln(y), y(0) = 1.$$

Solve the following first-order linear ODEs:

(12) 
$$dy/dx = -2y + 2xe^{-2x}$$
.

$$(13) dy/dx + y \tan(x) = \sin(x).$$