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Hybrid (discrete+continuous) networksDiscrete (Subsidy? and Buys?); continuous (Harvest and Cost)Subsidy? and Buys?); continuous (Harvest and Cost)Subsidy? (furge)Subsidy? (furge)Subsidy? (furge)SupportOption 1: discretization—possibly large errors, large CPTsOption 2: finitely parameterized canonical families1) Continuous variable, discrete+continuous parents (e.g., Cost)2) Discrete variable, continuous parents (e.g., Buys?)	Compact conditional distributions CPT grows exponentially with number of parents CPT becomes infinite with continuous-valued parent or child Solution: canonical distributions that are defined compactly Deterministic nodes are the simplest case: $X = f(Parents(X))$ for some function f E.g., Boolean functions NorthAmerican \Leftrightarrow Canadian $\lor US \lor Mexican$ E.g., numerical relationships among continuous variables $\frac{\partial Level}{\partial t}$ = inflow + precipitation - outflow - evaporation	Example: Car diagnosic Initial evidence: car won't start Testable variables (green), 'broken, so fix it' variables (gray) ensure sparse structure, reduce parameters Imitian evidence: car won't start Initian variables (grean), 'broken, so fix it' variables (orange) Initian variables (gray) ensure sparse structure, reduce parameters Imitian variables (gray) Imitian evidence: car won't start Initian variables (gray) Imitian evidence: car won't start
Continuous child variablesNeed one conditional density function for child variable given continuous parents, for each possible assignment to discrete parentsMost common is the linear Gaussian model, e.g.,: $P(Cost = c Harvest = h, Subsidy? = true)$ $= N(a_th + b_t, \sigma_t)(c)$ $= \frac{1}{\sigma_t \sqrt{2\pi}} exp \left(-\frac{1}{2} \left(\frac{c - (a_t h + b_t)}{\sigma_t} \right)^2 \right)$ Mean Cost varies linearly with Harvest, variance is fixedLinear variation is unreasonable over the full range but works OK if the likely range of Harvest is narrow	Compact conditional distributions contd.Noisy-OR distributions model multiple noninteracting causes 1) Parents $U_1 \dots U_k$ include all causes (can add leak node) 2) Independent failure probability q_i for each cause alone $\Rightarrow P(X U_1 \dots U_{j_1} \neg U_{j_1+1} \dots \neg U_k) = 1 - \prod_{i=1}^{j} q_i$ Cold Flu Malaria $P(Fever)$ F F F T F T F T F T F T F T $Gold$ $D.0$ T T F 0.9 0.0 0.1 F T T T T T 0.98 $0.02 = 0.2 \times 0.1$ T T T 0.94 $0.06 = 0.6 \times 0.2$ $0.12 = 0.6 \times 0.2 \times 0.1$ T T T T T 0.988 $0.12 = 0.6 \times 0.2 \times 0.1$ T T T 0.988 $0.12 = 0.6 \times 0.2 \times 0.1$ T T T T T T T 0.988 $0.12 = 0.6 \times 0.2 \times 0.1$	Image: Caring in the second

Summary Bayes nets provide a natural representation for (causally induced) conditional independence Topology + CPTs = compact representation of joint distribution Generally easy for (non)experts to construct Canonical distributions (e.g., noisy-OR) = compact representation of CPTs Continuous variables ⇒ parameterized distributions (e.g., linear Gaussian)	Why the probit? 1. It's sort of the right shape 2. Can view as hard threshold whose location is subject to noise Image: I	Continuous child variablesNurse of the provide
	$\label{eq:constant} \begin{tabular}{lllllllllllllllllllllllllllllllllll$	eq:probability of Buys? given Cost should be a "soft" threshol: $ $

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