



Code Generation I

- Stack machines
- The MIPS assembly language
- A simple source language
- Stack-machine implementation of the simple language
- Readings: 9.1-9.7

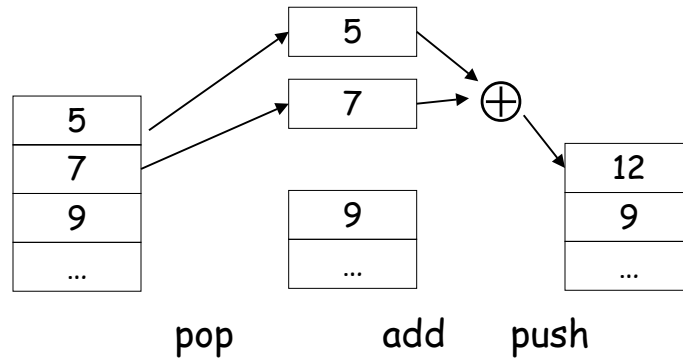


Stack Machines

- A simple evaluation model
- No variables or registers
- A stack of values for intermediate results
- Each instruction:
 - Takes its operands from the top of the stack
 - Removes those operands from the stack
 - Computes the required operation on them
 - Pushes the result on the stack

Example of Stack Machine Operation

- The addition operation on a stack machine



Example of a Stack Machine Program

- Consider two instructions
 - push i - place the integer i on top of the stack
 - add - pop two elements, add them and put the result back on the stack
- A program to compute $7 + 5$:
 - push 7
 - push 5
 - add



Why Use a Stack Machine ?

- Each operation takes operands from the same place and puts results in the same place
- This means a uniform compilation scheme
- And therefore a simpler compiler



Why Use a Stack Machine ?

- Location of the operands is implicit
 - Always on the top of the stack
- No need to specify operands explicitly
- No need to specify the location of the result
- Instruction "add" as opposed to "add r_1, r_2 "
 - ⇒ Smaller encoding of instructions
 - ⇒ More compact programs
- This is one reason why Java Bytecodes use a stack evaluation model



Optimizing the Stack Machine

- The add instruction does 3 memory operations
 - Two reads and one write to the stack
 - The top of the stack is frequently accessed
- Idea: keep the top of the stack in a register (called accumulator)
 - Register accesses are faster
- The "add" instruction is now
$$\text{acc} \leftarrow \text{acc} + \text{top_of_stack}$$
 - Only one memory operation!



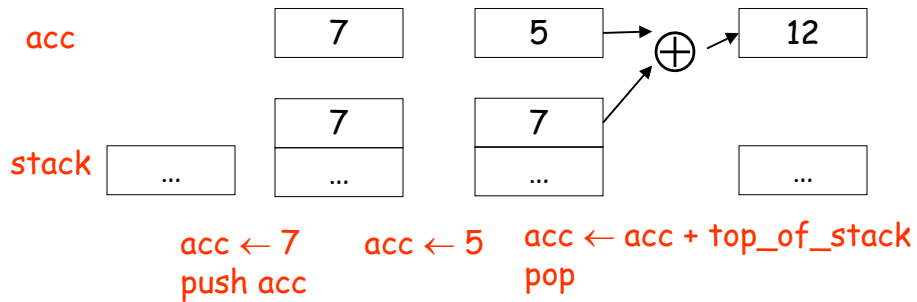
Stack Machine with Accumulator

Invariants

- The result of computing an expression is always in the accumulator
- For an operation $op(e_1, \dots, e_n)$ push the accumulator on the stack after computing each of e_1, \dots, e_{n-1}
 - After the operation pop $n-1$ values
- After computing an expression the stack is as before

Stack Machine with Accumulator. Example

- Compute $7 + 5$ using an accumulator



A Bigger Example: $3 + (7 + 5)$

Code	Acc	Stack
<code>acc ← 3</code>	3	<init>
<code>push acc</code>	3	3, <init>
<code>acc ← 7</code>	7	3, <init>
<code>push acc</code>	7	7, 3, <init>
<code>acc ← 5</code>	5	7, 3, <init>
<code>acc ← acc + top_of_stack</code>	12	7, 3, <init>
<code>pop</code>	12	3, <init>
<code>acc ← acc + top_of_stack</code>	15	3, <init>
<code>pop</code>	15	<init>



Notes

- It is very important that the stack is preserved across the evaluation of a subexpression
 - Stack before the evaluation of $7 + 5$ is 3, <init>
 - Stack after the evaluation of $7 + 5$ is 3, <init>
 - The first operand is on top of the stack



From Stack Machines to MIPS

- The compiler generates code for a stack machine with accumulator
- We want to run the resulting code on the MIPS processor (or simulator)
- We simulate stack machine instructions using MIPS instructions and registers



Simulating a Stack Machine...

- The accumulator is kept in MIPS register `$a0`
- The stack is kept in memory
- The stack grows towards lower addresses
 - Standard convention on the MIPS architecture
- The address of the next location on the stack is kept in MIPS register `$sp`
 - The top of the stack is at address `$sp + 4`



MIPS Assembly

MIPS architecture

- Prototypical Reduced Instruction Set Computer (RISC) architecture
- Arithmetic operations use registers for operands and results
- Must use load and store instructions to use operands and results in memory
- 32 general purpose registers (32 bits each)
 - We will use `$sp`, `$a0` and `$t1` (a temporary register)



A Sample of MIPS Instructions

- `lw reg1 offset(reg2)`
 - Load 32-bit word from address `reg2 + offset` into `reg1`
- `add reg1 reg2 reg3`
 - `reg1 ← reg2 + reg3`
- `sw reg1 offset(reg2)`
 - Store 32-bit word in `reg1` at address `reg2 + offset`
- `addiu reg1 reg2 imm`
 - `reg1 ← reg2 + imm`
 - "u" means overflow is not checked
- `li reg imm`
 - `reg ← imm`



MIPS Assembly. Example.

- The stack-machine code for `7 + 5` in MIPS:

<code>acc ← 7</code>	<code>li \$a0 7</code>
<code>push acc</code>	<code>sw \$a0 0(\$sp)</code>
	<code>addiu \$sp \$sp -4</code>
<code>acc ← 5</code>	<code>li \$a0 5</code>
<code>acc ← acc + top_of_stack</code>	<code>lw \$t1 4(\$sp)</code>
	<code>add \$a0 \$a0 \$t1</code>
<code>pop</code>	<code>addiu \$sp \$sp 4</code>

- We now generalize this to a simple language...



A Small Language

- A language with integers and integer operations

$P \rightarrow D; P \mid D$

$D \rightarrow \text{def id(ARGS) = E};$

$\text{ARGS} \rightarrow \text{id}, \text{ARGS} \mid \text{id}$

$E \rightarrow \text{int} \mid \text{id} \mid \text{if } E_1 = E_2 \text{ then } E_3 \text{ else } E_4$
 $\mid E_1 + E_2 \mid E_1 - E_2 \mid \text{id}(E_1, \dots, E_n)$



A Small Language (Cont.)

- The first function definition f is the “main” routine
- Running the program on input i means computing $f(i)$
- Program for computing the Fibonacci numbers:

$\text{def fib}(x) = \text{if } x = 1 \text{ then } 0 \text{ else}$
 $\quad \text{if } x = 2 \text{ then } 1 \text{ else}$
 $\quad \text{fib}(x - 1) + \text{fib}(x - 2)$



Code Generation Strategy

- For each expression e we generate MIPS code that:
 - Computes the value of e in $\$a0$
 - Preserves $\$sp$ and the contents of the stack
- We define a code generation function $cgen(e)$ whose result is the code generated for e



Code Generation for Constants

- The code to evaluate a constant simply copies it into the accumulator:

$$cgen(i) = li \$a0 i$$

- Note that this also preserves the stack, as required



Code Generation for Add

```
cgen( $e_1 + e_2$ ) =  
  cgen( $e_1$ )  
  sw $a0 0($sp)  
  addiu $sp $sp -4  
  cgen( $e_2$ )  
  lw $t1 4($sp)  
  add $a0 $t1 $a0  
  addiu $sp $sp 4
```

- Possible optimization: Put the result of e_1 directly in register $\$t1$?



Code Generation for Add. Wrong!

- Optimization: Put the result of e_1 directly in $\$t1$?

```
cgen( $e_1 + e_2$ ) =  
  cgen( $e_1$ )  
  move $t1 $a0  
  cgen( $e_2$ )  
  add $a0 $t1 $a0
```

- Try to generate code for : $3 + (7 + 5)$



Code Generation Notes

- The code for `+` is a template with “holes” for code for evaluating e_1 and e_2
- Stack machine code generation is recursive
- Code for $e_1 + e_2$ consists of code for e_1 and e_2 glued together
- Code generation can be written as a recursive-descent of the AST
 - At least for expressions



Code Generation for Sub and Constants

- New instruction: `sub reg1 reg2 reg3`
 - Implements $\text{reg}_1 \leftarrow \text{reg}_2 - \text{reg}_3$

```
cgen(e1 - e2) =  
  cgen(e1)  
  sw $a0 0($sp)  
  addiu $sp $sp -4  
  cgen(e2)  
  lw $t1 4($sp)  
  sub $a0 $t1 $a0  
  addiu $sp $sp 4
```



Code Generation for Conditional

- We need flow control instructions
- New instruction: **beq reg₁ reg₂ label**
 - Branch to label if reg₁ = reg₂
- New instruction: **b label**
 - Unconditional jump to label



Code Generation for If (Cont.)

```
cgen(if e1 = e2 then e3 else e4) =  
  cgen(e1)  
  sw $a0 0($sp)  
  addiu $sp $sp -4  
  cgen(e2)  
  lw $t1 4($sp)  
  addiu $sp $sp 4  
  beq $a0 $t1 true_branch  
false_branch:  
  cgen(e4)  
  b end_if  
true_branch:  
  cgen(e3)  
end_if:
```



The Activation Record

- Code for function calls and function definitions depends on the layout of the activation record
- A very simple AR suffices for this language:
 - The result is always in the accumulator
 - No need to store the result in the AR
 - The activation record holds actual parameters
 - For $f(x_1, \dots, x_n)$ push x_n, \dots, x_1 on the stack
 - These are the only variables in this language



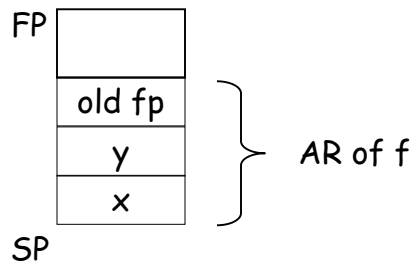
The Activation Record (Cont.)

- The stack discipline guarantees that on function exit $\$sp$ is the same as it was on function entry
 - No need for a control link
- We need the return address
- It's handy to have a pointer to the current activation
 - This pointer lives in register $\$fp$ (frame pointer)
 - Reason for frame pointer will be clear shortly



The Activation Record

- Summary: For this language, an AR with the caller's frame pointer, the actual parameters, and the return address suffices
- Picture: Consider a call to $f(x,y)$, The AR will be:



Code Generation for Function Call

- The calling sequence is the instructions (of both caller and callee) to set up a function invocation
- New instruction: **jal label**
 - Jump to label, save address of next instruction in $\$ra$
 - On other architectures the return address is stored on the stack by the "call" instruction



Code Generation for Function Call (Cont.)

```
cgen(f(e1,...,en)) =  
  sw $fp 0($sp)  
  addiu $sp $sp -4  
  cgen(en)  
  sw $a0 0($sp)  
  addiu $sp $sp -4  
  ...  
  cgen(e1)  
  sw $a0 0($sp)  
  addiu $sp $sp -4  
  jal f_entry
```

- The caller saves its value of the frame pointer
- Then it saves the actual parameters in reverse order
- The caller saves the return address in register **\$ra**
- The AR so far is **4*n+4** bytes long



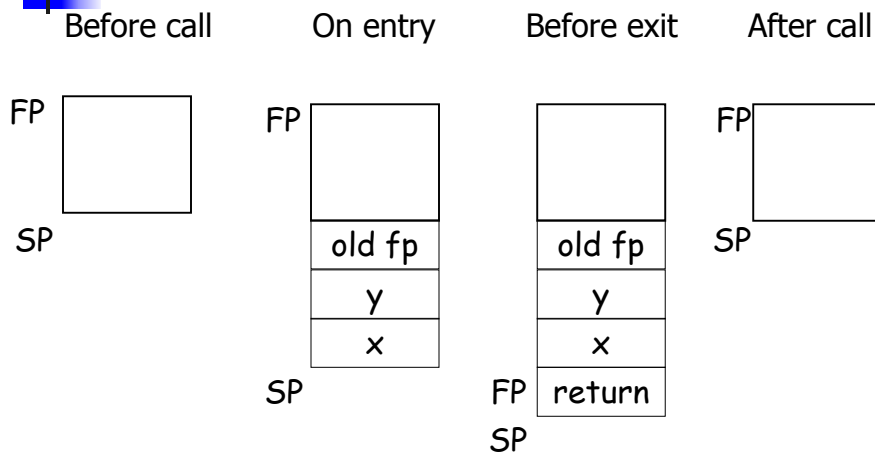
Code Generation for Function Definition

- New instruction: **jr reg**
 - Jump to address in register reg

```
cgen(def f(x1,...,xn) = e) =  
  move $fp $sp  
  sw $ra 0($sp)  
  addiu $sp $sp -4  
  cgen(e)  
  lw $ra 4($sp)  
  addiu $sp $sp z  
  lw $fp 0($sp)  
  jr $ra
```

- Note: The frame pointer points to the top, not bottom of the frame
- The callee pops the return address, the actual arguments and the saved value of the frame pointer
- **z = 4*n + 8**

Calling Sequence. Example for $f(x,y)$.



Code Generation for Variables

- Variable references are the last construct
- The "variables" of a function are just its parameters
 - They are all in the AR
 - Pushed by the caller
- Problem: Because the stack grows when intermediate results are saved, the variables are not at a fixed offset from $\$sp$

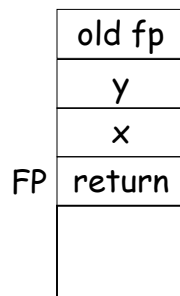
Code Generation for Variables (Cont.)

- Solution: use a frame pointer
 - Always points to the return address on the stack
 - Since it does not move it can be used to find the variables
- Let x_i be the i^{th} ($i = 1, \dots, n$) formal parameter of the function for which code is being generated

$\text{cgen}(x_i) = \text{lw } \$a0 \text{ z}(\$fp) \quad (z = 4*i)$

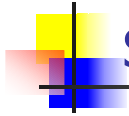
Code Generation for Variables (Cont.)

- Example: For a function $\text{def } f(x,y) = e$ the activation and frame pointer are set up as follows:



SP

- X is at $fp + 4$
- Y is at $fp + 8$



Summary

- The activation record must be designed together with the code generator
- Code generation can be done by recursive traversal of the AST
- Production compilers do different things
 - Emphasis is on keeping values (esp. current stack frame) in registers
 - Intermediate results are laid out in the AR, not pushed and popped from the stack
- Next time: code generation for objects