## Constructing SLR states

- LR(0) state machine
- encodes all strings that are valid on the stack
- each valid string is a configuration, and hence corresponds to a state of the LR(0) state machine
- each state tells us what to do (shift or reduce?)


## Constructing SLR states

- How to find the set of needed configurations
- What are the valid handles that can appear at the front of the input?
- Begin with item $S^{\prime} \rightarrow$. Start, calculate related items (closure)
- Determine following states (what states can be reached on a single input or nonterminal)
- Construct closure of each resulting state


## Closure of a Set of Items

closure (items $i$, grammar $g$ )
$c=i$
repeat
for each item $X \rightarrow \alpha . Y \beta$ in $c$ and each production $Y \rightarrow \gamma$ from $g$ s.t.
$Y \rightarrow . \gamma$ is not in $c$ add $Y \rightarrow, \gamma$ to $c$
until no further changes to $c$
return $c$

## Closure Example

- Grammar

$$
\begin{aligned}
& \mathrm{E} \rightarrow \mathrm{~T}+\mathrm{E} \mid \mathrm{T} \\
& \mathrm{~T} \rightarrow \text { int * } \mathrm{T} \mid \text { int | (E) }
\end{aligned}
$$

- Initial item $\mathrm{S}^{\prime} \rightarrow$. E
- $c=\left\{\mathrm{S}^{\prime} \rightarrow\right.$. E$\}$
- First pass $\{S \rightarrow$.E $\}$
- Add $\mathrm{E} \rightarrow$. $\mathrm{T}+\mathrm{E} \quad c=\left\{\mathrm{S}^{\prime} \rightarrow \mathrm{E}, \mathrm{E} \rightarrow . \mathrm{T}+\mathrm{E}\right\}$
- Add $\mathrm{E} \rightarrow$. $\mathrm{T} \quad c=\left\{\mathrm{S}^{\prime} \rightarrow \mathrm{E}, \mathrm{E} \rightarrow . \mathrm{T}+\mathrm{E}, \mathrm{E} \rightarrow . \mathrm{T}\right\}$
- Second pass $c=\left\{\mathrm{S}^{\prime} \rightarrow \mathrm{E}, \mathrm{E} \rightarrow . \mathrm{T}+\mathrm{E}, \mathrm{E} \rightarrow . \mathrm{T}\right\}$
- Add $T \rightarrow$. int $* T c=\left\{S^{\prime} \rightarrow . E, E \rightarrow . T+E, E \rightarrow . T, T \rightarrow\right.$. int $\left.* T\right\}$
- Add $\mathrm{T} \rightarrow$. int $\quad c=\left\{\mathrm{S}^{\prime} \rightarrow \mathrm{E}, \mathrm{E} \rightarrow . \mathrm{T}+\mathrm{E}, \mathrm{E} \rightarrow . \mathrm{T}, \mathrm{T} \rightarrow\right.$.int $* \mathrm{~T}, \mathrm{~T} \rightarrow$.int $\}$
- Add $\mathrm{T} \rightarrow$. (E) $\quad c=\left\{\mathrm{S}^{\prime} \rightarrow . \mathrm{E}, \mathrm{E} \rightarrow . \mathrm{T}+\mathrm{E}, \mathrm{E} \rightarrow . \mathrm{T}, \mathrm{T} \rightarrow\right.$.int*T,T $\rightarrow$.int , $\mathrm{T} \rightarrow$.(E) $\}$
- Third pass $c=\left\{\mathrm{S}^{\prime} \rightarrow . \mathrm{E}, \mathrm{E} \rightarrow . \mathrm{T}+\mathrm{E}, \mathrm{E} \rightarrow . \mathrm{T}, \mathrm{T} \rightarrow\right.$.int*T,T $\rightarrow$.int , $\mathrm{T} \rightarrow$.(E) $\}$
- no change


## Closure Example

- Closure results in a new state
- Closure of $\left\{S^{\prime} \rightarrow\right.$. $E$ \} is
$\left\{S^{\prime} \rightarrow . E, E \rightarrow . T+E, E \rightarrow . T, T \rightarrow\right.$. int*T,
$\mathrm{T} \rightarrow$.int , $\mathrm{T} \rightarrow$.( E$)\}$

| $S^{\prime} \rightarrow . E \quad 1$ |
| :--- |
| $E \rightarrow . T$ |
| $E \rightarrow . T+E$ |
| $T \rightarrow .(E)$ |
| $T \rightarrow$ int * $T$ |
| $T \rightarrow$ int |

## New States - the goto Function

- To determine possible states reachable from existing state use goto function
- goto(state,stack element) is the closure of the set of items that result from shifting stack element in state
- For state $\left\{\mathrm{S}^{\prime} \rightarrow \mathrm{E}, \mathrm{E} \rightarrow . \mathrm{T}+\mathrm{E}, \mathrm{E} \rightarrow . \mathrm{T}, \mathrm{T} \rightarrow\right.$.int*T,

$$
\mathrm{T} \rightarrow \text {.int , } \mathrm{T} \rightarrow \text {.(E) \} }
$$

set of items resulting from shifting int are:
$\{\mathrm{T} \rightarrow$ int. , $\mathrm{T} \rightarrow$ int.$* T\}$

## Goto Function

goto (items i, stackel J, grammar $g$ )
initial= set of items $X \rightarrow \alpha J$. $\beta$ such that $X \rightarrow \alpha . J \beta$ is in $i$ return closure(initial, $g$ )

## Producing Set of States

calc_states (grammar $g$ )
$s t s=\left\{\right.$ closure $\left(\left\{\left[S^{\prime}->\right.\right.\right.$. Start $\left.\left.\left.]\right\}, g\right)\right\}$
repeat
for each state $s$ in $s t s$ and each stack element $e$ such that goto $(s, e)$ is not empty and not in sts add goto( $s, e)$ to $s t s$
until no more states can be added to sts

## Defining SLR States Example <br> - Grammar

$$
\begin{aligned}
& \mathrm{E} \rightarrow \mathrm{~T}+\mathrm{E} \mid \mathrm{T} \\
& \mathrm{~T} \rightarrow \text { int } * \mathrm{~T} \mid \text { int } \mid(\mathrm{E})
\end{aligned}
$$

- Initial state:

$$
\begin{aligned}
& \hline S^{\prime} \rightarrow . E \\
& E \rightarrow . T \\
& E \rightarrow . T+E \\
& T \rightarrow .(E) \\
& T \rightarrow \text {.int } * T \\
& T \rightarrow . \text { int } \\
& \hline
\end{aligned}
$$

## States Example (cont)

From initial state (1) From state 1 on $T$ we get on E we get state 2 state 3


## States Example (cont)



## States Example (cont)

From state 3 on + we From state 4 on $E$ we get get state 6

## States Example (cont)

From state 4 on $T$ we From state 4 on (we get get state 3 state 4


## States Example (cont)

From state 4 on int we get state 5
$T \rightarrow$ int
$T \rightarrow$ int


## States Example (cont)

From state 6 on E we From state 6 on T we get get state 9 state 3


## States Example (cont)

From state 6 on ( we From state 6 on int we get get state 4 state 5

| $E \rightarrow T+$ E 6 | $\mathrm{T} \rightarrow$ (. E) |
| :---: | :---: |
| $E \rightarrow . T$ | $E \rightarrow . T$ |
| $E \rightarrow . T+E$ | ( E $\rightarrow$. T + E |
| $T \rightarrow$ (E) | $T \rightarrow$ (E) |
| $T \rightarrow$ int * $T$ | $T \rightarrow$ int * $T$ |
| $T \rightarrow$ int | $T \rightarrow$ int |


| $E \rightarrow T+$ E 6 |  |
| :---: | :---: |
| $E \rightarrow$. $T$ |  |
| $\mathrm{E} \rightarrow . \mathrm{T}+\mathrm{E}$ | int $\mathrm{T} \rightarrow$ int. * T |
| $\mathrm{T} \rightarrow$. E$)$ | T $\rightarrow$ int. 5 |
| $T \rightarrow$ int * $T$ |  |
| T $\rightarrow$. int |  |

States Example (cont)
From state 7 on ) we From state 8 on $T$ we get get state 10 state 11


States Example (cont)
From state 8 on ( we From state 8 on int we get get state 4 state 5



## Constructing an SLR Parse Table

- Add an extra production $\mathrm{S}^{\prime} \rightarrow$ Start to the grammar
- Construct set of $\operatorname{LR}(0)$ States, the initial state is the one containing $\mathrm{S}^{\prime} \rightarrow$. Start
- For each transition $\mathrm{A} \rightarrow{ }^{\mathrm{X}} \mathrm{B}$ in the set of states add an action shift $B$ in column $X$ for row $A$
- For each item $[Y \rightarrow \alpha$.] part of state $A$, set the action in row $A$ to reduce $Y \rightarrow \alpha$ for each column $X$ in FOLLOW(Y)
- Empty table items are errors
- Grammar is not SLR if more than one entry for any table item


## Resulting SLR Parse Table

|  | int | * | + | ( | ) | \$ | E | T |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 1 | s5 |  |  | s4 |  |  | s2 | s3 |
| 2 |  |  |  |  |  | acc |  |  |
| 3 |  |  | s6 |  | r2 | r2 |  |  |
| 4 | s5 |  |  | s4 |  |  | s7 | s3 |
| 5 |  | s8 | r4 |  | r4 | r4 |  |  |
| 6 | s5 |  |  | s4 |  |  | s9 | s3 |
| 7 |  |  |  |  | s10 |  |  |  |
| 8 | s5 |  |  | s4 |  |  |  | s11 |
| 9 |  |  |  |  | r1 | r1 |  |  |
| 10 |  |  | r5 |  | r5 | r5 |  |  |
| 11 |  |  | r3 |  | r3 | r3 |  |  |

1: $\mathrm{E} \rightarrow \mathrm{T}+\mathrm{E}$
2: $\mathrm{E} \rightarrow \mathrm{T}$
3: $\mathrm{T} \rightarrow$ int * T
4: $T \rightarrow$ int
5: $T \rightarrow(E)$

## Another Example

Grammar: $S \rightarrow A x B|B \quad A \rightarrow y B| z \quad B \rightarrow A$


## Corresponding Parse Table

|  | X | y | Z | \$ | S | A | B |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 1 |  | s5 | s6 |  | s2 | s3 | s4 |
| 2 |  |  |  | acc |  |  |  |
| 3 | $\begin{aligned} & \text { s8, } \\ & \text { r5 } \end{aligned}$ |  |  | r5 |  |  |  |
| 4 |  |  |  | r2 |  |  |  |
| 5 |  | s5 | s6 |  |  | s7 | s9 |
| 6 | r4 |  |  | r4 |  |  |  |
| 7 | r5 |  |  | r5 |  |  |  |
| 8 |  | s5 | s6 |  |  | S7 | S10 |
| 9 | r3 |  |  | r3 |  |  |  |
| 10 |  |  |  | r1 |  |  |  |

Follow $(S)=\{\$\}$
Follow $(A)=\{x, \$\}$
Follow $(B)=\{x, \$\}$

1: $S \rightarrow A x B$
2: $S \rightarrow B$
3: $A \rightarrow y B$
4: $\mathrm{A} \rightarrow \mathrm{Z}$
5: $B \rightarrow A$

## Limits of SLR Parsing

- But is it really possible to get to state 3 through a B - no, the only viable prefix involves an A !
- So the reduce is a bad choice
- Limit introduced by SLR parsing in using the FOLLOW set to decide reductions
- Idea: augment LR items with 1 character lookahead [ S $\rightarrow$. AxB , b ] making an $\operatorname{LR}(1)$ item


## Canonical LR Parsing

- States similar to SLR, but use LR(1) rather than LR(0) items
- When reduction is possible, use reduction of an item [ $S \rightarrow \alpha ., x$ ] only when next token is $x$ (lookahead items used only for reductions)
- Advantage: avoids some conflicts introduced by SLR parsing tables
- Disadvantage: table is often MUCH larger as items are differentiated by which character currently used for lookahead
- Building LR(1) tables - similar to SLR, only need change closure and goto functions


## Look Ahead LR (LALR) Parsing

- Disadvantage of large tables can be mitigated by merging states
- States can be merged when there is no fundamental difference
- E.g., similar states with no reductions possible with different lookahead characters

